

Obavezan domaći zadatak – korenovanje

Zadaci za ocene 3 i 4

ZADATAK 1. Izračunaj:

$$a) \sqrt{45} + \sqrt{12} - (\sqrt{48} + \sqrt{125}) + \sqrt{20},$$

$$b) 3\sqrt{4a} - 5\sqrt{12a} + 5\sqrt{9a} + 2\sqrt{75a} - 2\sqrt{81a},$$

$$c) \sqrt[3]{\frac{64a^2b^2(a+b)^3}{c^2}} + 2 \cdot \sqrt[3]{\frac{27a^5b^2}{c^2}} - 2 \cdot \sqrt[3]{\frac{8a^2b^5}{c^2}}.$$

ZADATAK 2. Uprosti izraze:

$$a) (\sqrt{5} - 2\sqrt{3})(\sqrt{5} + 2\sqrt{3}) - (\sqrt{3} + 2\sqrt{5})(\sqrt{3} - 2\sqrt{5}),$$

$$b) \sqrt[3]{\frac{1}{2} + \frac{2}{5}} \cdot \sqrt[3]{3 \cdot \left(\frac{1}{4} + \frac{2}{7}\right)} \cdot \sqrt[3]{5 \cdot \left(\frac{1}{4} + \frac{1}{3}\right)},$$

$$c) \sqrt{\frac{1}{x+y} + \frac{2y}{x^2-y^2}} \cdot \sqrt{\frac{1}{x+y}} \cdot \sqrt{\frac{x^2}{y^2} - 1}.$$

ZADATAK 3. Ako su $A = \sqrt[3]{xy\sqrt{xy}} \cdot \sqrt{xy \cdot \sqrt[3]{\frac{1}{xy}}}$ i $B = \sqrt{xy} \cdot \sqrt{x \cdot \sqrt[3]{\frac{1}{y}}} \cdot \sqrt{y \cdot \sqrt[3]{\frac{1}{x}}}$ tada je $A = B$.

Dokaži.

ZADATAK 4. Izračunaj $\left(5^{\frac{1}{3}} + 3^{\frac{1}{3}}\right) \cdot \left(5^{\frac{2}{3}} - 15^{\frac{1}{3}} + 3^{\frac{2}{3}}\right)$.

ZADATAK 5. Racionališi:

$$a) \frac{10}{\sqrt{7} - \sqrt{2}}$$

$$b) \frac{xy}{\sqrt[9]{x^5}}$$

$$c) \frac{5}{\sqrt[3]{2} + \sqrt[3]{3}}$$

ZADATAK 6. Koristeći Lagranžov identitet izračunaj:

a) $\sqrt{6 + \sqrt{20}}$

b) $\sqrt{6 - 4\sqrt{2}}$